

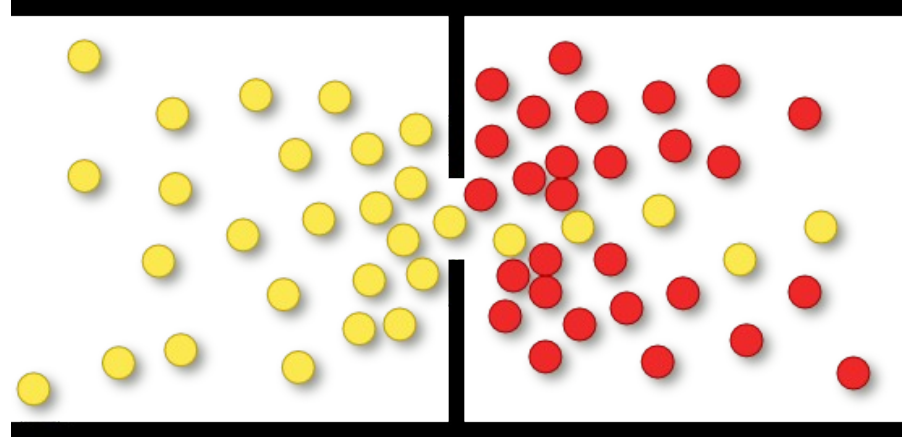
Mobile Robots and Autonomous Vehicles

Week 5: Behavior Modeling and Learning

- Other approaches: Social Forces

Social Forces Model

- Reactive approach for crowd simulation
- Models interactions within people
- Does not depend on the environment
- Intended destination has to be estimated somehow



Social Forces: general algorithm

- At every time step:
 - Compute the total force for each agent i :

$$m_i \frac{dv_i}{dt} = m_i \frac{\hat{v}_i(t)\hat{e}_i(t) - v_i(t)}{\tau} + \sum_{j \neq i} f_{ij} + \sum_w f_{iw}$$

- Compute acceleration and update the agent's position

Social Forces: general algorithm

Desired motion

- At every time step:
 - Compute the total force for each agent i :

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Other pedestrians

Social Forces: general algorithm

Desired motion

- At every time step:

- Compute the total force for each agent i :

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Static obstacles

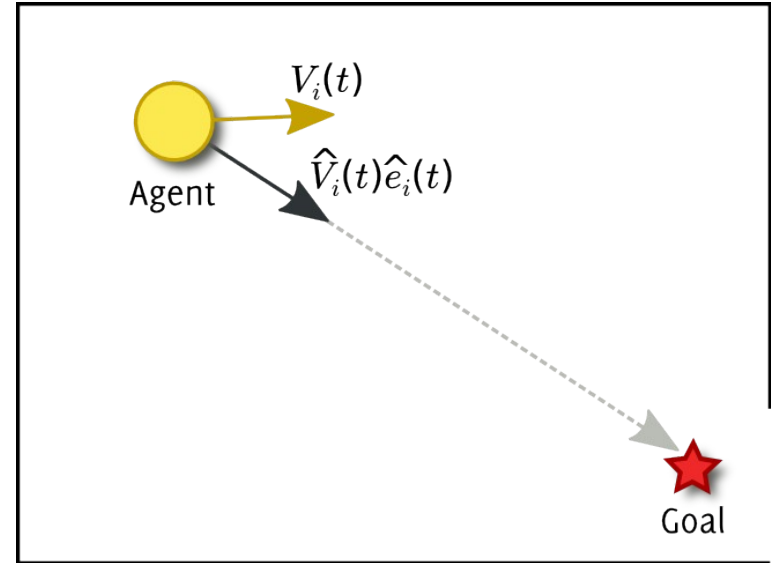
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Other pedestrians

Social Forces: desired motion

$$m_i \frac{\hat{v}_i(t)\hat{e}_i(t) - v_i(t)}{\tau}$$

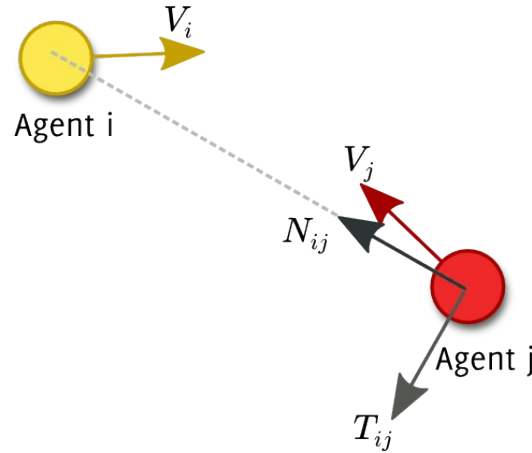
- m_i : Agent's mass
- $\hat{v}_i(t)$: Desired direction
- $\hat{e}_i(t)$: Desired speed
- $v_i(t)$: Actual velocity
- τ : Time interval



Social Forces: pedestrian interaction

$$F_{ij} = \{ae^{(r_{ij}-d_{ij})/b} + kg(r_{ij} - d_{ij})\}N_{ij} + \kappa g(r_{ij} - d_{ij})\Delta v_{ji}T_{ij}$$

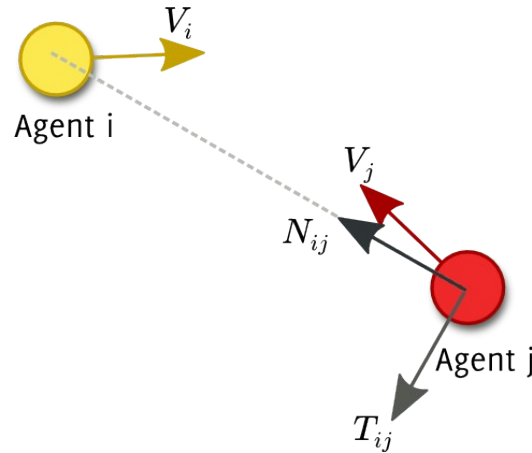
- a, b, k, κ : tuning variables
- d_{ij} : agent distance
- r_{ij} : sum of agents' radius
- N_{ij} : relative direction from j to i
- $g(x)$: x if colliding, 0 otherwise
- T_{ij} : tangential direction
- v_{ji} : tangential velocity difference



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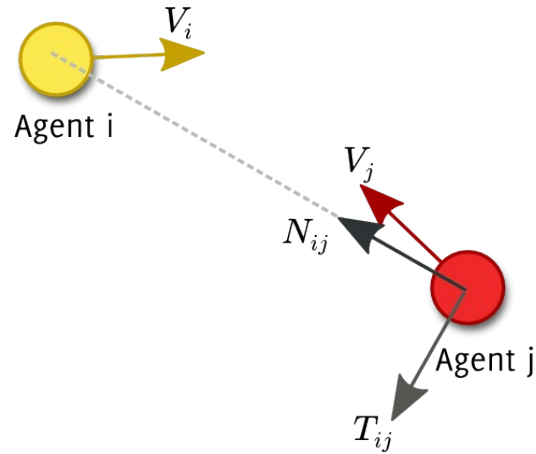
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Collision avoidance

Non-penetration



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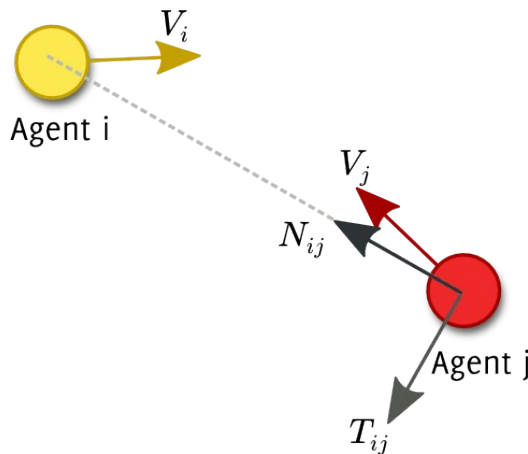
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Collision avoidance

Non-penetration

Sliding force

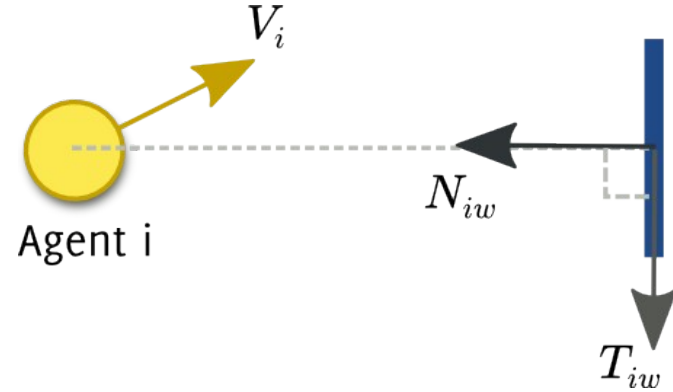
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Social Forces: static interaction

$$F_{iw} = \{ae^{(r_i - d_{iw})/b} + kg(r_i - d_{iw})\}N_{iw} + \kappa g(r_i - d_{iw})(v_i \cdot T_{iw})T_{iw}$$

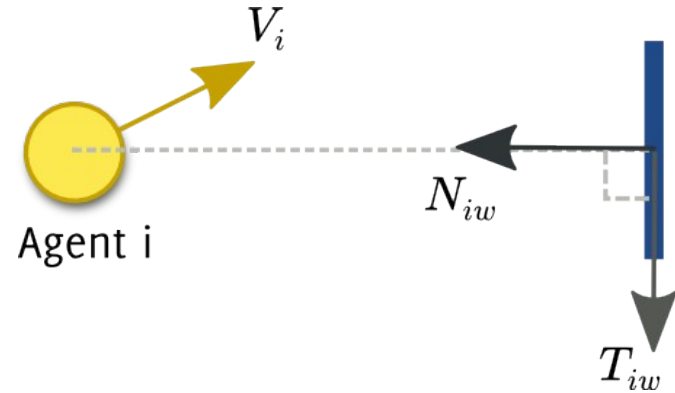
- a, b, k, κ : tuning variables
- d_{iw} : wall distance
- r_i : agent's radius
- N_{iw} : relative direction from wall
- $g(x)$: x if colliding, 0 otherwise
- T_{iw} : tangential direction
- v_i : agent's velocity



Social Forces: static interaction

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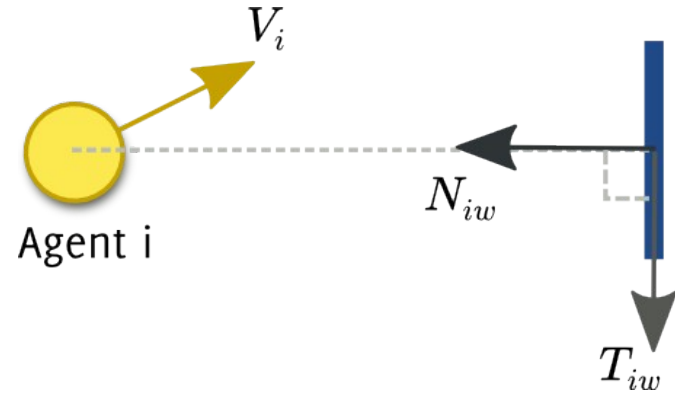
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- a, b, k, κ : tuning variables
 - Collision avoidance
 - Non-penetration
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Social Forces: static interaction

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- a, b, k, κ : tuning variables

Collision avoidance

Non-penetration

Sliding force

- d_{iw} : wall distance

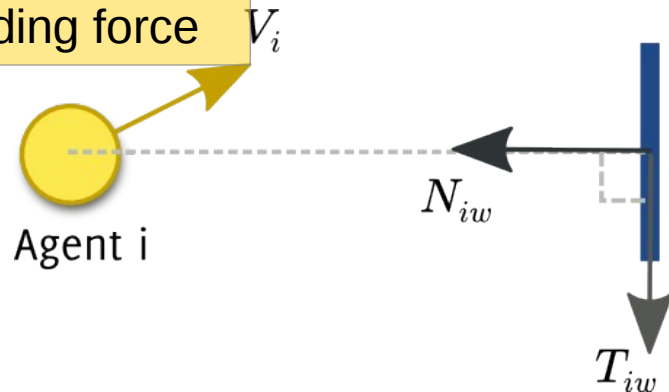
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- v_i : agent's velocity



Social Forces vs. HMMs

HMMs

- ✓ Infers intentions
- ✓ Long-term prediction
- ✗ Requires robust data association
- ✗ Requires global perception
- ✗ Does not model person to person interaction
- ✗ Only for original environment

Social Forces

- ✓ Models person to person and person to environment interactions
- ✓ Works on any environment
- ✓ Does not require robust data association.
- ✗ Does not infer intention
- ✗ Only short-term predictions